

# YEAR 8

# KNOWLEDGE

# ORGANISERS



## AUTUMN TERM 1

# RATIO & PROPORTION

*Unit 1: Ratio & Scale*

*Unit 2: Multiplicative Change*

*Unit 3: Ratio & Proportion Problems*

# RATIO & PROPORTION...

## Unit 1: Ratio and Scale



### What do I need to be able to do?

By the end of this unit you should be able to:

- Simplify any given ratio
  - Share an amount in a given ratio
  - Solve ratio problems given a part
- Solutions should be modelled, explained and solved.

### Keywords

**Ratio:** a statement of how two numbers compare

**Part:** a section of a whole

**Equivalent:** of equal value

**Factors:** integers that multiply together to get the original value

**Scale:** the ratio between the small version and its actual size.

**Circumference:** The perimeter of a circle

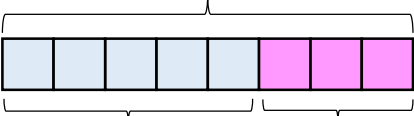
**Radius:** The distance from the centre to the outside of a circle

**Diameter:** The distance right across a circle, through the centre

### Representing a ratio

"For every 5 boys there are 3 girls"

This is the "whole" – boys and girls together

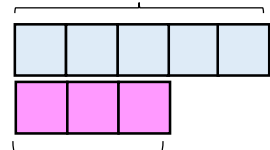


This represents the 5 boys

This represents the 3 girls

5:3

This represents the 5 boys



This represents the 3 girls

This is the "whole" – boys and girls together

### Order is Important

"For every dog there are 2 cats"



Dogs: Cats

1:2

The ratio has to be written in the same order as the information is given.

e.g. 2:1 would represent 2 dogs for every 1 cat. ✗

### Simplifying a ratio

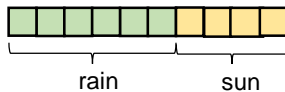
Cancel down the ratio to its lowest form

"For every 6 days of rain there are 4 days of sun"

6:4

÷ 2 ↓

3:2



"For every 3 days of rain there are 2 days of sun" – when this happens twice the ratio becomes 6:4.

### Ratio 1:n (or n:1)

This is asking you to cancel down until the part indicated represents 1.

Show the ratio 4:20 in the ratio of 1:n

The question states that this part has to be 1 unit. Therefore Divide by 4

4:20  
↓  
1:5

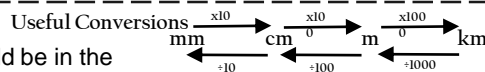
This side has to be divided by 4 too – to keep in proportion

\*H\* the n part does not have to be an integer for this type of question

### Units are important:

When using a ratio – all parts should be in the

same units

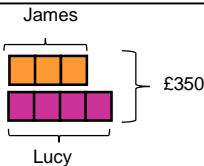


### Sharing a whole into a given ratio

James and Lucy share £350 in the ratio 3:4. Work out how much each person earns

#### Model the Question

James : Lucy  
3 : 4



#### Find the value of one part (one box)

Whole: £350  
7 parts to share between (3 James, 4 Lucy)  
£350 ÷ 7 = £50  
□ = one part = £50

#### Put back into the question

James: Lucy  
3 : 4  
(x 50) (x 50)  
£150:£200

James = 3 x £50 = £150  
Lucy = 4 x £50 = £200

### Finding a value given 1:n (or n:1)

Inside a box are blue and red pens in the ratio 5:1. If there are 10 red pens how many blue pens are there?

#### Model the Question

Blue : Red  
5 : 1

□ = one part = 10 pens



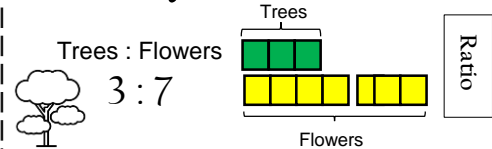
#### Put back into the question

Blue : Red  
5 : 1  
(x 10) (x 10)  
50 : 10

Blue pens = 5 x 10 = 50 pens  
Red pens = 1 x 10 = 10 pens

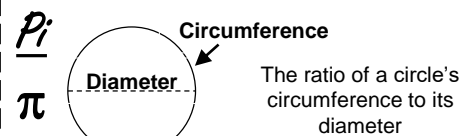
There are 50 Blue Pens

### Ratio as a fraction



#### Fraction of trees

Number of parts of in group: 3  
Total number of parts: 10  
Tree parts 3 + Flower parts 7 = 10



# RATIO & PROPORTION...

## Unit 2: Multiplicative Change

### What do I need to be able to do?

By the end of this unit you should be able to:

- Solve problems and explain direct proportion
- Use conversion graphs to make statements, comparisons and form conclusions.
- Understand and use scale factors for length

### Keywords

- Variable:** a part or letter where the value can be changed
- Axes:** horizontal and vertical lines that a graph is plotted around
- Approximation:** an estimate for a value
- Similar Shapes:** Shapes that are in the same ratio – one is an enlargement of the other.
- Scale Factor:** the multiple that increases the size of a shape
- Currency:** the system of money used in a particular country
- Conversion:** the process of changing one variable to another
- Scale:** the ratio between the small version and its actual size.

### Direct Proportion

As one variable changes the other changes at the same rate.



4 cans of pop = £2.40

This is a multiplicative change

4 cans of pop = £2.40

12 cans of pop = £7.20

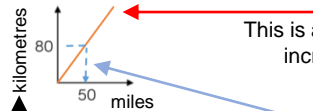
4 cans of pop = £2.40  
 $\times 0.5$   
 2 cans of pop = £1.20

This multiplier is the same  
 In the same way that this would be for ratio

Sometimes this is easiest if you work out how much one unit is worth first  
 e.g. 1 can of pop = £0.60

### Conversion Graphs

Compare two variables



This is always a straight line because as one variable increases so does the other at the same rate

Labelling of both axes is vital

To make conversions between units you need to find the point to compare – then find the associated point by using your graph. Using a ruler helps for accuracy. Showing your conversion lines help as a “check” for solutions

### Conversion between currencies



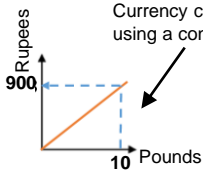
£1 = 90 Rupees

Currency is directly proportional

For every £1 I have 90 Rupees

£1 = 90 Rupees  
 $\times 10$   
 £10 = 900 Rupees

Currency can be converted using a conversion graph



Convert 630 Rupees into Pounds

£1 = 90 Rupees  
 $\times 7$   
 £7 = 630 Rupees

### Ratio between similar shapes



Angles in similar shapes do not change. e.g. if a triangle gets bigger the angles can not go above 180°

The two rectangles are similar.



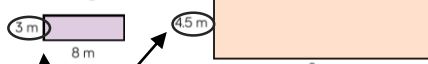
Corresponding sides

$\div 3$   $3m : 4.5m$   $\div 3$   $\times 8$   $8m : 12m$   $\times 8$   $1m : 1.5m$   $\times 8$

Note: Simplify to the same ratio

### Understand Scale

The two rectangles are similar.



$$3 \times 1.5 = 4.5$$

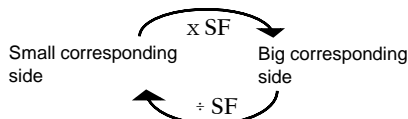
This is a multiplicative change

Missing length  
 $8 \times 1.5 = 12m$

Use corresponding sides to calculate a scale factor

Scale factor can be calculated by:

**Bigger corresponding side**  
**Smaller corresponding side**



### Draw and interpret scale diagrams

A picture of a car is drawn with a scale of 1:30

For every 1cm on my image is 30cm in real life

The car image is 10cm

Image : Real life  
 1cm : 30cm  
 $\times 10$   $10cm : 300cm$   $\times 10$

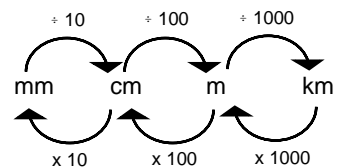


The car in real life is 210cm

Image : Real life  
 1cm : 30cm  
 $\times 7$   $7cm : 210cm$   $\times 7$



### Interpret maps with scale factors



1 cm : 250 m

Ratios need to be in the same units

1 cm : 250m

$250 \times 100 = 25000$   
 1 cm : 25000cm

For every 1cm on my map is 25000cm in real life.



# RATIO & PROPORTION...

## Unit 3: Solving Ratio & Proportion Problems

### What do I need to be able to do?

By the end of this unit you should be able to:

- Understand and solve problems with variables in direct proportion.
- Recognise direct proportion graphs and use conversion graphs.
- Understand and solve problems with variables in inverse proportion.
- Recognise inverse proportion graphs.
- Solve ratio problems
- Solve Best Buy problems

### Keywords

**Variable:** a part or letter where the value can be changed

**Direct Proportion:** When two variables are connected so that if you double one variable, then you also double the other.

**Inverse Proportion:** When two variables are connected so that if you double one variable, then you halve the other.

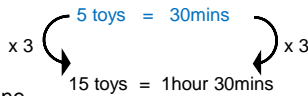
**Conversion:** the process of changing one variable to another

**Origin:** the point (0,0) on a graph

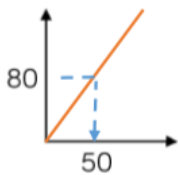
### Direct Proportion

As one variable changes the other changes at the same rate. So if one variable doubles, so does the other.

It takes a man 30mins to make 5 toys.  
How long will it take him to make 15 toys?



A graph of direct proportion is a straight line going through the origin.

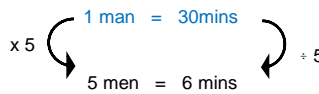


To make conversions between units you need to find the point to compare then find the associated point by using your graph. If the numbers go off the scale you can use a number that is on the graph and then multiply both by 10, 100 etc

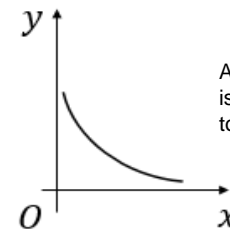
### Inverse Proportion

As one variable changes the other changes in the opposite way. So if one variable doubles, the other one halves.

It takes a man 30mins to make 5 toys.  
How long will it take 5 men to make the 5 toys?



If there are MORE men, it will take LESS time



A graph of inverse proportion is a curve like this. It never touches either axis.

### Ratio Problems

James and Lucy share some money in the ratio 3:5. Lucy gets £30 more than James. Work out how much each person gets

#### Model the Question

James : Lucy  
3 : 5

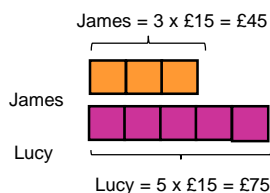


#### Find the value of one part (one box)

Lucy gets 2 parts more which is £30 more so  $£30 = 2$  parts (2 boxes)  
1 parts =  $£30 \div 2 = £15$

$£30 \div 2 = £15$   
□ = one part = £15

#### Put back into the question



### Best Buy Problems

Which tube is the best value for money?

250 ml  
£2

300 ml  
£2.50

#### Method 1 - ml per £

Small tube  
 $£2 = 250\text{ml}$   
 $£1 = 250 \div 2 = 125\text{ml per } £1$

Big tube  
 $£2.50 = 300\text{ml}$   
 $£1 = 300 \div 2.5 = 120\text{ml per } £1$

So the small tube better value (get more toothpaste per £)

#### Method 2 - cost per ml

Small tube  
 $250\text{ml} = £2 = 200\text{p}$   
 $1\text{ml} = 200 \div 250 = 0.8\text{p per ml}$

Big tube  
 $300\text{ml} = £2.50 = 250\text{p}$   
 $1\text{ml} = 250 \div 300 = 0.8333\text{p per ml}$

So the small tube better value (costs less per ml)